

#### AFRICAN ECONOMIC RESEARCH CONSORTIUM

# Collaborative PhD Programme in Economics for Sub-Saharan Africa COMPREHENSIVE EXAMINATIONS IN CORE AND ELECTIVE FIELDS FEBRUARY 13 – MARCH 3, 2017

## MICROECONOMICS

Time: 08:00 – 11:00 GMT

Date: Friday, February 17, 2017

#### **INSTRUCTIONS:**

Answer a total of FOUR questions: ONE question from Section A, ONE question from Section B, and TWO questions from Section C. Please note that **Question 5** in Section C is **COMPULSORY**.

The sections are weighted as indicated on the paper.

## Section A: (15%)

#### Answer only ONE Question from this Section

#### **Question 1**

Explain why demand curves slope down to the right for all normal goods and some inferior goods. [15 Marks]

#### **Question 2**

(a) Using a graph, explain the relation between average and marginal cost curves.

[7 Marks]

(b) In a competitive market in the short run, state and explain the condition under which a firm produces a positive output level. [8 Marks]



## **Section B: (25%)**

### Answer only ONE Question from this Section

### **Question 3**

A production function for a perfectly competitive firm is given as:

$$q = A x_1^{\frac{1}{2}} x_2^{\frac{1}{2}}$$

where q is the output (in tons) and  $x_i$  are amounts of inputs used in the production process. The cost of producing q is given by:

$$C = \sum_{i} w_i x_i , \quad i = 1, 2$$

where  $w_i$  are per unit input prices for input 1 and input 2.

- (a) Derive the cost function in its general form and verify that it satisfies the homogeneity property and Shephard's Lemma. [10 Marks]
- (b) When  $w_1 = w_2 = 100$  and A=10, what is the minimum amount of each input required to produce 360 tons of output? [5 Marks]
- (c) Compute the optimal profit for the firm when p = 20. [2 Marks]
- (d) Compare and contrast the Cobb Douglas and constant elasticity of substitution (CES) production functions. [8 Marks]

## **Question 4**

Consider an economy with two consumers A and B. Consumers A and B have utility functions  $u(x_1^A, x_2^A) = (x_1^A)^{1/4} (x_2^A)^{1/2}$  and  $u(x_1^B, x_2^B) = (x_1^B)^{1/4} (x_2^B)^{1/2}$ , respectively. They face prices  $p_1$  and  $p_2$  for good 1 and good 2, respectively, and they have incomes  $I^A$  and  $I^B$ , respectively.

- (a) Write formally the economic problem faced by consumer A and derive the Marshallian demand functions  $x_1^{*A}(p_1, p_2, I^A)$  and  $x_2^{*A}(p_1, p_2, I^A)$ . [5 Marks]
- (b) Explain Walras' Law. Why is this law important for the general equilibrium theory? [8 Marks]
- (c) If the consumers have initial endowments  $e^{A} = (3,3)$  and  $e^{B} = (9,6)$ , compute the Walrasian equilibrium relative price, and allocations. [12 Marks]



## **Section C: (60%)**

# Answer TWO Questions from this Section, One of which MUST be Question 5, which is COMPULSORY

### **Question 5 (Compulsory)**

For each of the following statements define the underlined terms then determine whether the statement is **True, False or Uncertain** with a brief explanation of your answer. Answer **any five** of the sub-questions in this question.

- (a) The <u>Kuhn Tucker conditions</u> are valid only for solving <u>constrained optimization</u> <u>problems</u> with boundary conditions. [6 Marks]
- (b) A <u>risk averse agent</u> will always prefer the <u>expected value</u> of a gamble for sure than the gamble itself. [6 Marks]
- (c) <u>Hotelling's lemma</u> allows us to derive the <u>supply function</u> from the profit function [6 Marks]
- (d) If a <u>natural monopoly</u> is to operate at the efficient output level by adopting <u>marginal</u> <u>cost pricing</u>, it will need a subsidy to stay in production. [6 Marks]
- (e) In the <u>repeated prisoner's dilemma game</u> the <u>Folk theorem</u> provides the necessary condition for the Pareto efficient outcome to be sustainable. [6 Marks]
- (f) <u>Equivalent variation</u> and <u>Compensating Variation</u> always give identical measurements of welfare changes. [6 Marks]
- (g) In the presence of <u>negative externalities</u> a firm will produce more than the <u>socially</u> <u>optimal output</u>. [6 Marks]
- (h) The <u>lemon market</u> of Akerlof illustrates <u>a moral hazard</u> problem. [6 Marks]



#### **Question 6**

Consider the following indirect utility function derived from a consumer's utility maximization:

$$v(p, y) = \alpha_1 \left(\frac{y}{p_1}\right)^{\beta_1} + \alpha_2 \left(\frac{y}{p_2}\right)^{\beta_2}$$

where y is income,  $p_i$  is price of commodity i, for i = 1, 2. and  $\alpha_i$  and  $\beta_i$  are parameters.

(a)	Determine the Lagrange multiplier of the underlying consumer's utility problem.	maximization [8 Marks]
(b)	Determine the Marshallian demand functions.	[12 Marks]
(c)	Explain the concept of duality in consumer theory.	[10 Marks]

#### **Question 7**

Two friends, *Juma* and *Amina*, are considering a time out together and need to take decisions simultaneously on what activity to engage in. *Juma* loves visiting (V), *Amina* loves the theater (T). The payoff to each from choosing either of the two activities given the choice of the other is represented in the game matrix below

Amina		
Juma	V	Τ
V	3, 1	0, 0
Т	0, 0	2, 5

- (a) Identify the pure strategy Nash equilibrium (equilibria) if any. [3 Marks]
- (b) Is there any Nash equilibrium in mixed strategies? If yes derive the mixed strategy Nash equilibrium. [5 Marks]
- (c) Draw the extensive form of the game and determine which of the pure strategy Nash equilibria is credible. [7 Marks]
- (d) Game theory has become a major tool of analysis in economics. Provide a critique of this approach. [15 Marks]



#### **Question 8**

Consider the following principal-agent situation. We have a principal P and an agent A. P wants to hire A for a one time project. If A works for P, A can choose high effort,  $e_H$ , or low effort,  $e_L$ . Profits are either high,  $\pi_H$ , or low  $\pi_L$ , with  $\pi_H > \pi_L$ . If A chooses  $e_H$ then profits are  $\pi_H$  with probability  $\rho_H$ , and  $\pi_L$  with probability  $1 - \rho_H$ . If A chooses  $e_L$  then profits are  $\pi_H$  with probability  $\rho_L$  and  $\pi_L$  with probability  $1 - \rho_L$ . P maximizes expected profits from the project, less the expected wages paid to the agent, A maximizes expected utility as follows, given a wage, w, and effort choice, e: U(w,e) = V(w) - e where V'(w) > 0 and V''(w) < 0. P designs a contract, A then accepts it or not, and if A accepts, A then chooses an effort level. Assume that A has a reservation utility level of  $U_0$ .

- (a) Show how to implement  $e_L$  and  $e_H$  if effort is observable and verifiable and the agent is risk averse. [10 Marks]
- (b) Answer part (a) above given that the agent is risk neutral. [5 Marks]
- (c) If *e* is not observable, and the agent is risk-neutral, show that P can still obtain the same payoffs as in case (a). [15 Marks]